culations have led to a new understanding of the mechanism of cyclopropane ring openings by palladium(II), and it is found that exactly the opposite to what was previously thought is true. The conclusion is that corner activation is the favored pathway, especially when the metal has the possibility to ionize into a cationic complex. Instead it is the edge pathway that needs special cir-
cumstances to become available
Acknowledgment. We thank Eva Björkman for her contribution to the calculations presented in this paper.

Registry No. $\mathrm{C}_{3} \mathrm{H}_{6}, 75-19-4 ; \mathrm{PdCl}_{2}, 7647-10-1 ; \mathrm{PdCl}_{4}$, 14349-67-8; $\mathrm{PdCl}^{+}, 19651-81-1$.

# Rate Constant for Cyclization/Decyclization of the Phenyl Radical 

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#### Abstract

Formation of cyclic $\mathrm{C}_{6} \mathrm{H}_{5}$ from ${ }^{\circ} \mathrm{CH}=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}-\mathrm{C} \equiv \mathrm{CH}$ was investigated by means of the MINDO/3 parametrization of SCF-MO theory and RRKM calculations of the unimolecular rate constants for both directions of reaction.


We report a theoretical study of the formation of phenyl radical by attack of a terminal vinyl radical upon a terminal ethynyl group (Figure 1), a reaction of importance in soot nucleation. ${ }^{1}$

## Procedure

Structures and energies were computed by the MINDO/3 method with the MOPAC programs. ${ }^{2}$ Standard MOPAC options were used for locating the transition structure ${ }^{3}$ and for computing force constants and vibrational frequencies. No constraints were used except for imposing planarity on the phenyl radical.

Rate constants for unimolecular isomerizations require an extension of standard RRKM theory. ${ }^{4}$ For incorporation into a modeling program the conversion from the open-chain radical (OC) to the phenyl radical $(P R)$ has to be described by a kinetic equation

$$
\begin{equation*}
-\frac{\mathrm{d}[\mathrm{OC}]}{\mathrm{d} t}=k_{\mathrm{f}}[\mathrm{OC}]-k_{\mathrm{r}}[\mathrm{PR}] \tag{1}
\end{equation*}
$$

The corresponding formulation of the unimolecular process is written

$$
\begin{equation*}
\mathrm{OC} \underset{k_{-1}[\mathrm{M}]}{\stackrel{k_{1}[\mathrm{M}]}{\longrightarrow}} \mathrm{OC}^{*} \stackrel{k(E)}{\underset{k^{\prime}(E)}{\stackrel{k}{2}}} \mathrm{PR}^{*} \underset{k^{[ }[\mathrm{M}]}{\stackrel{\mathrm{K}^{\prime}}{ }[\mathrm{M}]} \mathrm{PR} \tag{2}
\end{equation*}
$$

and the expression for $k_{\mathrm{f}}$ is

$$
\begin{equation*}
k_{\mathrm{f}}=\int_{E_{0}}^{\infty} \frac{B(E) k(E) \mathrm{d} E}{1+\frac{k(E)}{k_{-1}[\mathrm{M}]}+\frac{k^{\prime}(E)}{k_{-1}^{\prime}[\mathrm{M}]}} \tag{3}
\end{equation*}
$$

where $B(E)$ is the Boltzmann distribution of molecules and $k(E)$ is the RRKM energy dependent unimolecular rate constant.

Direct counts of densities and numbers of states were used for computing $k(E)$ from the MINDO/3 vibrational frequencies. The path degeneracy is 1 for isomerization of OC and 2 for isomerization of PR. Collision diameters were taken to be 0.53 nm for $O C$ and $P R$ and 0.34

[^0]Table I. Molecular Properties Computed by the MINDO/3 Method Hexa-1,3-dien-5-yn-yl radical
Standard Enthalpy of Formation: $116.8 \mathrm{kcal} / \mathrm{mol}$
Moments of Inertia: ${ }^{a} A=117.7, B=356.6, C=474.3$

| Vibration $^{\text {Frequencies } b}$ |  |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 72 | 111 | 252 | 253 | 424 | 415 | 593 | 616 | 677 |
| 692 | 710 | 760 | 796 | 844 | 957 | 1089 | 1131 | 1184 |
| 1352 | 1584 | 1720 | 2311 | 3275 | 3421 | 3440 | 3640 | 3795 |

Phenyl Radical
Standard Enthalpy of Formation: $69.6 \mathrm{kcal} / \mathrm{mol}$
Moments of Inertia: $A=134.9, B=153.6, C=288.4$
Vibration Frequencies

| 372 | 408 | 523 | 552 | 558 | 682 | 782 | 805 | 827 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 840 | 849 | 1031 | 1045 | 1089 | 1092 | 1152 | 1154 | 1238 |
| 1442 | 1457 | 1589 | 1686 | 3477 | 3484 | 3497 | 3518 | 3521 |

Standard Enthalpy of Formation: $133.4 \mathrm{kcal} / \mathrm{mol}$
Moments of Inertia: $A=149.6, B=183.1, C=332.7$
Vibration Frequencies

| $-424^{c}$ | 230 | 301 | 308 | 440 | 462 | 613 | 666 | 682 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 717 | 750 | 765 | 823 | 866 | 1047 | 1080 | 1094 | 1171 |
| 1362 | 1456 | 1644 | 2057 | 3374 | 3475 | 3512 | 3582 | 3732 |

${ }^{a}$ Units $\mathrm{g} \mathrm{cm}^{2} \times 10^{40}$. ${ }^{b}$ Units $\mathrm{cm}^{-1}$. ${ }^{c}$ Reaction coordinate.
nm for $\mathbf{M}$, as estimates appropriate to reaction in Ar buffer gas; the corresponding collision diameter for $\mathrm{PR}-\mathrm{Ar}$ and $\mathrm{OC}-\mathrm{Ar}$ collisions is then
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Figure 1. Computed structures for open chain, transition structure, and phenyl radicals.


Figure 2. Falloff of unimolecular rate constant at 1500 (upper), 2000, and 2500 K .
0.43 nm . The remaining molecular properties were taken from the MINDO/3 calculations.

## Results and Discussion

The structures computed by MINDO/3 for the three species of interest are shown in Figure 1. Molecular properties are given in Table I. Except for the heats of formation, discussed below, the molecular properties are unremarkable. The low-frequency vibrational modes of the open-chain radical were treated as true vibrations in the rate constant calculation even though they are clearly reflecting the presence of an essentially free rotation.
The unimolecular rate constants computed for 1500,2000 , and 2500 K are shown for a range of pressures in Table II and Figure 2. For the temperature and pressure range of shock-tube experiments on soot formation in $\mathrm{C}_{2} \mathrm{H}_{2}-\mathrm{Ar}$ mixtures the computed rate constants are about an order of magnitude lower than the $10^{10} \mathrm{~s}^{-1}$ value used in simulations. ${ }^{1}$ This difference would change the computed soot yield values by no more than a factor somewhere between 2 and 4 for pyrolysis of acetylene, depending on the thermochemical data adopted, less for other pyrolytic soot sources, and far less in an oxidizing environment. The falloff curves (Figure 2) are typical for molecules of this size for these conditions. ${ }^{4}$

Because of the high degree of reversibility within the sootforming reactions, equilibrium constants prove to be more important than rate constants in determining the course of reaction. Equilibrium constants for use in computer simulations were computed with thermochemical data derived from group-additivity estimates. ${ }^{6}$ For the parametrization used these implied enthalpy changes of $112 \mathrm{kcal} / \mathrm{mol}$ for removal of an H atom from benzene and $48 \mathrm{kcal} / \mathrm{mol}$ for opening the phenyl ring compared to the MINDO/3 values of 93 and $47 \mathrm{kcal} / \mathrm{mol}$, respectively. It is of interest to inquire as to the source of the large difference in the

[^1]Table II. Unimolecular Rate Constants

| $P^{a}$ | $k(\mathrm{PR} \rightarrow \mathrm{OC})^{\mathrm{b}}$ | $k(\mathrm{OC} \rightarrow \mathrm{PR})^{b}$ | $k / k_{\infty}$ | order | $(E\rangle^{c}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1500 \mathrm{~K} ;\langle E\rangle$ of Energized Molecules $=1.03 \times 10^{4}$;$K_{\text {eq }}(\mathrm{OC} \rightarrow \mathrm{PR})=1800$ |  |  |  |  |  |
| 380 | $1.6 \times 10^{5}$ | $2.9 \times 10^{8}$ | 0.42 |  | $1.32 \times 10^{4}$ |
| 760 | $2.1 \times 10^{5}$ | $3.8 \times 10^{8}$ | 0.55 | 1.39 | $1.38 \times 10^{4}$ |
| 1520 | $2.6 \times 10^{5}$ | $4.7 \times 10^{8}$ | 0.68 | 1.29 | $1.43 \times 10^{4}$ |
| 3040 | $3.0 \times 10^{5}$ | $5.4 \times 10^{8}$ | 0.79 | 1.21 | $1.48 \times 10^{4}$ |
| $\infty$ | $3.8 \times 10^{5}$ | $6.9 \times 10^{8}$ | 1.0 | 1 | $1.59 \times 10^{4}$ |
| $\begin{gathered} 2000 \mathrm{~K} ;\langle E\rangle \text { of Energized Molecules }=1.83 \times 10^{4} ; \\ K_{\mathrm{eq}}(\mathrm{OC} \rightarrow \mathrm{PR})=26 \end{gathered}$ |  |  |  |  |  |
| 380 | $1.5 \times 10^{7}$ | $3.8 \times 10^{8}$ | 0.14 |  | $1.77 \times 10^{4}$ |
| 760 | $2.3 \times 10^{7}$ | $6.0 \times 10^{8}$ | 0.22 | 1.64 | $1.85 \times 10^{4}$ |
| 1520 | $3.4 \times 10^{7}$ | $8.7 \times 10^{8}$ | 0.32 | 1.55 | $1.92 \times 10^{4}$ |
| 3040 | $4.6 \times 10^{7}$ | $1.2 \times 10^{9}$ | 0.44 | 1.45 | $2.01 \times 10^{4}$ |
| $\infty$ | $1.1 \times 10^{8}$ | $2.7 \times 10^{9}$ | 1.0 | 1 | $2.4 \times 10^{4}$ |
| $2500 \mathrm{~K} ;\langle E\rangle$ of Energized Molecules $=2.09 \times 10^{4}$; $K_{\text {eq }}(\mathrm{OC} \rightarrow \mathrm{PR})=2.1$ |  |  |  |  |  |
| 380 | $1.2 \times 10^{8}$ | $2.5 \times 10^{8}$ | 0.04 |  | $2.29 \times 10^{4}$ |
| 760 | $2.1 \times 10^{8}$ | $4.4 \times 10^{8}$ | 0.07 | 1.81 | $2.36 \times 10^{4}$ |
| 1520 | $0.5 \times 10^{8}$ | $7.3 \times 10^{8}$ | 0.12 | 1.74 | $2.45 \times 10^{4}$ |
| 3040 | $5.6 \times 10^{8}$ | $1.2 \times 10^{9}$ | 0.19 | 1.66 | $2.55 \times 10^{4}$ |
| $\infty$ | $3.0 \times 10^{9}$ | $6.2 \times 10^{9}$ | 1.0 | 1 | $3.3 \times 10^{4}$ |

${ }^{a}$ Units Torr. ${ }^{b}$ Units s ${ }^{-1}$. ${ }^{c}$ Units $\mathrm{cm}^{-1}$.
$\mathrm{C}-\mathrm{H}$ bond dissociation energy. The MINDO/ 3 value for the standard enthalpy of formation of phenyl radical ( $70 \mathrm{kcal} / \mathrm{mol}$ ) indicates greater stability than the experimental values of 78,80 , and $81 \mathrm{kcal} / \mathrm{mol}$ derived from kinetics experiments ${ }^{7-9}$ and 83 $\mathrm{kcal} / \mathrm{mol}$ derived from mass-spectrometric studies. ${ }^{10,11}$ The only other theoretical value of which we are aware is the BAC-MP4 result of $88 \mathrm{kcal} / \mathrm{mol} .{ }^{12}$ For benzene itself, MINDO $/ 3$ overestimates the standard enthalpy of formation, experimentally 20 $\mathrm{kcal} / \mathrm{mol}$, by $9 \mathrm{kcal} .{ }^{2}$ The apparently low C-H bond dissociation energy thus arises from an unusually large positive discrepancy in the MINDO/3 standard enthalpy of formation of benzene combined with an apparently low value for phenyl radical. In view of the uncertain experimental value ${ }^{7-11}$ it is clear that further theoretical and experimental study is justified. In computing the molecular properties in this study we had elected not to use the MNDO parametrization because of its known tendency to overestimate barriers to breaking $\mathrm{C}-\mathrm{C}$ bonds. ${ }^{13}$ After the rate constant calculations had been completed we were in a position to repeat the molecular properties calculation with the AM-1 parametrization, which gives the standard enthalpy of formation of benzene only $2 \mathrm{kcal} / \mathrm{mol}$ high. The computed enthalpies of formation of the open-chain radical, phenyl radical, and the transition structure proved to be 127,73 , and $146 \mathrm{kcal} / \mathrm{mol}$, respectively, with essentially identical geometries as computed by MINDO/3. This value for phenyl radical then implies an AM-1 value for the $\mathrm{C}-\mathrm{H}$ bond dissociation energy in benzene of 103 $\mathrm{kcal} / \mathrm{mol}, 10 \mathrm{kcal} / \mathrm{mol}$ above the MINDO $/ 3$ value. A $\mathrm{C}-\mathrm{H}$ bond dissociation energy lower than the $112 \mathrm{kcal} / \mathrm{mol}$ value used in the simulations would imply lower activation energies for H abstraction from aromatic rings and thus increase computed soot yields. The higher relative stability of phenyl radical compared to the open chain radical ( $54 \mathrm{kcal} / \mathrm{mol}$ for AM- 1 compared to $47 \mathrm{kcal} / \mathrm{mol}$ for MINDO $/ 3$ ) would, extended by analogy to the higher ring radicals, also increase computed soot yields.
Acknowledgment. This research was supported by the NASA-Lewis Research Center, the U.S.-Israel Binational Science Foundation, and the Robert A. Welch Foundation. We acknowledge the technical assistance of John Pojman.

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